

Please put away all papers and electronic devices except a calculator. Show enough work that it is clear how you arrived at your answer. Round decimal answers to four decimal places. Box/circle your final answers. Good luck!

1. (4 points) Fill in the correct frequencies in the frequency table below based on the following data.

31 32 5 3 2 9 10 15 43 12  
 7 28 39 11 46 18 20 37 49 0

Interval	Frequency
0-9	6
10-19	5
20-29	2
30-39	4
40-49	3

2. Consider the following set of data.

29 27 14 23 27

- (a) (4 points) Compute the mean  $\bar{x}$ , and show how you arrived at your answer.

$$\bar{x} = \frac{\sum x}{n} = \frac{29 + 27 + 14 + 23 + 27}{5}$$

$$= \frac{120}{5} = \boxed{24}$$

- (b) (4 points) Compute the median.

1. PUT IN ORDER

14 23  $\boxed{27}$  27 29

2. MIDDLE VALUE

- (c) (4 points) Compute the mode.

$\boxed{27}$

- (d) (4 points) Compute the range.

$$\text{HIGHEST} - \text{LOWEST} = 29 - 14 = \boxed{15}$$

TWO DIFFERENT  
WAYS

(e) (4 points) Compute the variance  $s^2$ , and show how you arrived at your answer.

$x$	$x - \bar{x}$	$(x - \bar{x})^2$
29	5	25
27	3	9
14	-10	100
23	-1	1
27	3	9
		144

$$s^2 = \frac{\sum (x - \bar{x})^2}{n - 1}$$

$$= \frac{144}{4}$$

$$= \boxed{36}$$

$x$	$x^2$
29	841
27	729
14	196
23	529
27	729
3024	

$$s^2 = \frac{\sum x^2 - n \bar{x}^2}{n - 1}$$

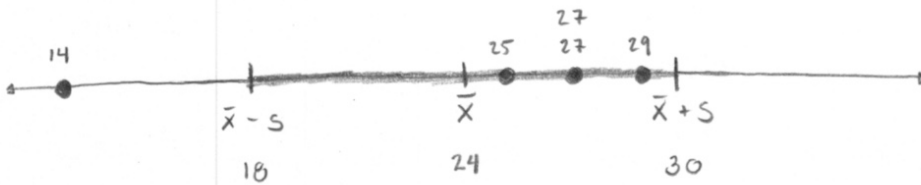
$$= \frac{3024 - 5(576)}{4}$$

$$= 36$$

(f) (4 points) Compute the standard deviation  $s$ , and show how you arrived at your answer.

$$s = \sqrt{s^2} = \sqrt{36} = \boxed{6}$$

(g) (4 points) What percentage of the data values lie within 1 standard deviation of the mean?

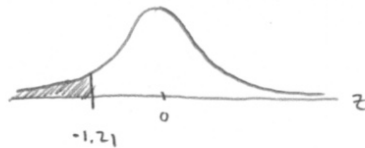


4 out of 5 DATA VALUES  
LIE WITHIN 1S OF  $\bar{x}$ ,  
i.e. BETWEEN 18 & 30.

$$\therefore \frac{4}{5} = \boxed{80\%}$$

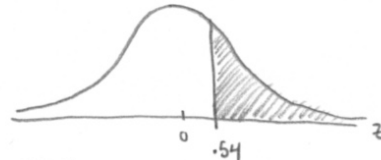
3. Let  $z$  be a random variable with the standard normal probability distribution ( $\mu = 0, \sigma = 1$ ). Using the table provided at the end of the exam or a calculator, determine the following probabilities.

(a) (8 points)  $P(z \leq -1.21)$



$$\boxed{.1131}$$

(b) (8 points)  $P(z \geq 0.54)$

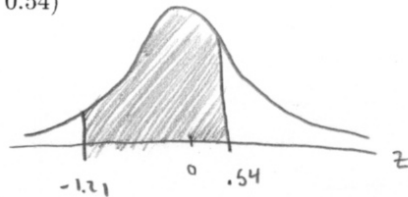


$$P(z \geq .54) = 1 - P(z \leq .54)$$

$$= 1 - .7054$$

$$= \boxed{.2946}$$

(c) (8 points)  $P(-1.21 \leq z \leq 0.54)$



$$P(-1.21 \leq z \leq .54)$$

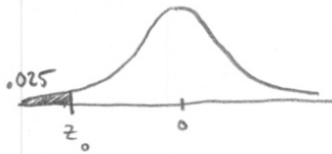
$$= P(z \leq .54) - P(z \leq -1.21)$$

$$= .7054 - .1131$$

$$= \boxed{.5923}$$

4. Let  $z$  be a random variable with the standard normal probability distribution ( $\mu = 0, \sigma = 1$ ). Use the table provided at the end of the exam or a calculator to answer the following questions.

(a) (8 points) Determine the value  $z_0$  such that  $P(z \leq z_0) = .025$ .

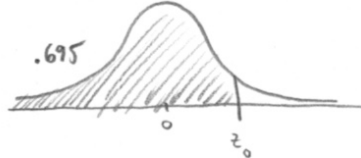


	.06
-1.9	.0250

$$z_0 = -1.96$$

(b) (8 points) Determine the value  $z_0$  such that  $P(z \geq z_0) = .305$ .

$$\begin{aligned} P(z \leq z_0) &= 1 - P(z \geq z_0) \\ &= 1 - .305 \\ &= .695 \end{aligned}$$



	.01
0.5	.6950

$$z_0 = .51$$

5. Suppose that you must establish regulations concerning the maximum number of people who can occupy an elevator. A study indicates that if eight people occupy the elevator, the probability distribution of the total weight  $x$  of the eight people is normally distributed with a mean  $\mu = 1200$  pounds and a standard deviation  $\sigma = 99$  pounds.

(a) (8 points) What is the probability that the total weight  $x$  of eight people exceeds 1425 pounds?

\* STANDARDIZE:  $z = \frac{x - \mu}{\sigma}$

$$P(x \geq 1425) = P\left(z \geq \frac{1425 - 1200}{99}\right) = P(z \geq 2.27)$$

$$= 1 - P(z \leq 2.27)$$

$$= 1 - .9884$$

(CALCULATOR ANSWER: .0115)

$$= .0116$$

(b) (8 points) Determine the value  $x_0$  such that the probability that the total weight  $x$  of the eight people exceeds  $x_0$  is .001.

FIRST FIND  $z_0$  SUCH THAT  $P(z \geq z_0) = .001 \iff P(z \leq z_0) = 1 - .001 = .999$

	.00
3.1	.9990

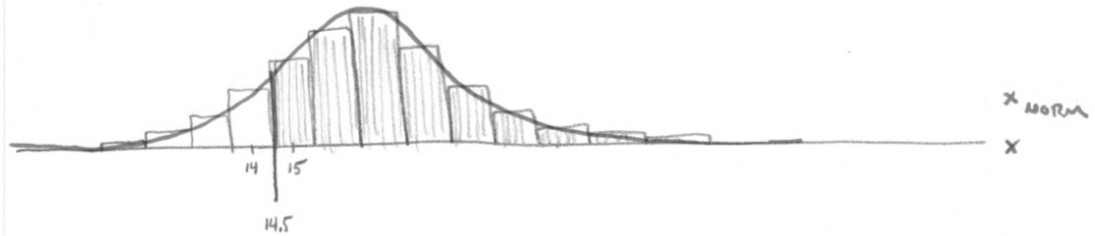
$$z_0 = 3.10 \text{ or } 3.09 \text{ or } 3.08$$

$$\text{THEN } z_0 = \frac{x_0 - \mu}{\sigma} \Rightarrow 3.1 = \frac{x_0 - 1200}{99}$$

$$x_0 = 1200 + (3.1)(99) = 1506.9 \quad \begin{matrix} \text{or } 1505.91 \\ \text{or } 1504.92 \end{matrix}$$

(CALCULATOR ANSWER: 1505.933)

6. (12 points) Airlines and hotels often grant reservations in excess of capacity to minimize losses due to no-shows. Suppose the records of a hotel show that, on the average,  $p = 10\%$  of their prospective guests will not claim their reservation (no-shows). If the hotel accepts  $n = 215$  reservations and there are only 200 rooms in the hotel, what is the probability that all guests who arrive to claim a room will receive one? In other words, what is the probability that the number of no-shows  $x$  is at least 15? Use a normal approximation to the binomial distribution for  $x$  to answer this question.



$$\mu = np = (215)(.1) = 21.5$$

$$\sigma = \sqrt{npq} = \sqrt{(215)(.1)(.9)} = 4.3989$$

$$P(x \geq 15) \approx P(x_{\text{NORM}} \geq 14.5)$$

↓ STANDARDIZE

$$= P(z \geq \frac{14.5 - 21.5}{4.3989}) = P(z \geq -1.59)$$

$$= 1 - P(z \leq -1.59)$$

$$= 1 - .0559$$

$$= \boxed{.9441}$$

$$\left( \begin{array}{l} \text{CALCULATOR} \\ \text{ANSWER} : .9442 \end{array} \right)$$