

Name: * Answer Key *
Math 150-E

Due 11/27/2019
Midterm Exam

Show enough work that it is clear how you arrived at your answer. Correct answers with no work shown will not receive full credit. Box/circle your final answers. Good luck!

5 pts

1. Draw a carefully labeled Venn diagram representing the premises below and state whether the argument is valid or invalid.

Premise: All pro athletes go to training camp.
Premise: Bruce Wayne doesn't go to training camp.
Conclusion: Bruce Wayne is not a pro athlete.



VALID

5 pts

2. A Boeing 747's fuel efficiency is approximately 0.2 miles per gallon. A Prius plug-in hybrid's fuel efficiency is approximately 50 miles per gallon. The distance from New York City to Miami is 1,091 miles. If the Boeing 747 carries 568 people and the Prius carries 2 people from New York City to Miami, calculate the gallons of fuel burned per person for each vehicle.

Boeing 747: $\frac{1 \text{ g}}{0.2 \text{ mi}} \cdot 1,091 \text{ mi} = 5455 \text{ g}$

$\frac{5455 \text{ g}}{568 \text{ people}} \approx 9.6039 \text{ g/person}$

Prius: $\frac{1 \text{ g}}{50 \text{ mi}} \cdot 1,091 \text{ mi} = 21.82 \text{ g}$

$\frac{21.82 \text{ g}}{2 \text{ people}} = 10.91 \text{ g/person}$

5 pts 3. If the bus fare in a certain city rose from 1.75 to 2.00, what percent increase would that be?

$$\text{PERCENT CHANGE} = \frac{\text{NEW} - \text{OLD}}{\text{OLD}} = \frac{2.00 - 1.75}{1.75} = \frac{.25}{1.75} = \frac{1}{7}$$

$$\approx .1429 \rightarrow$$

$$\boxed{14.29\%}$$

4 pts

4. Suppose you purchase a bag of coffee beans with a retail price of \$11.99. The local sales tax rate is 8.875%. What is the final cost? Round to the nearest cent.

PRICE INCREASES BY 8.875% \rightarrow MULTIPLY BY 1.08875

$$11.99 \times 1.08875 = 13.0541 \approx$$

$$\boxed{\$13.05}$$

5 pts

5. If the value of a pension fund rose 20% one year, and fell 8% the next, what was the net percentage increase over the 2-year period?

INCREASE BY 20%

DECREASE BY 8%

MULTIPLY BY 1.20

MULTIPLY BY .92

MULTIPLY BY BOTH

MULTIPLY BY

$$(1.20)(.92) = 1.104$$

\downarrow
INCREASE BY

$$\boxed{10.4\%}$$

6. A waiter earns \$400 per month (pre-tax) from an hourly wage and the rest of his pay is from tips. On average, he gets 20% of what a customer is charged in tips.

- 5 pts (a) Find a function that gives his total pay in a month as it varies with the total amount his customers are charged in that month.

Let $x = \text{TOTAL AMOUNT CUSTOMERS CHARGED}$
 $y = \text{TOTAL PAY}$

$$y = 400 + .2x$$

- 3 pts (b) If his customers are charged a total of \$5,500 in a month, what is his total (pre-tax) pay for that month?

Let $x = 5500$

$$y = 400 + .2(5500)$$

$$= 400 + 1100 = \$1500$$

- 3 pts (c) If he wants to make \$1,700 per month (pre-tax), how much does he need his customers to be charged per month?

Let $y = 1,700$

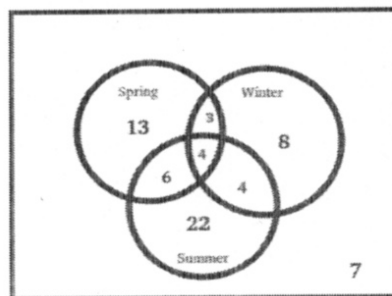
$$1,700 = 400 + .2x$$

$$1300 = .2x$$

$$\frac{1300}{.2} = x$$

$$x = \$6,500$$

7. In a recent survey people were asked if they took a vacation in the summer, winter, or spring in the past year. The results are summarized in the following Venn diagram.



- 2 pts (a) How many people took a vacation in only in the Summer? 22

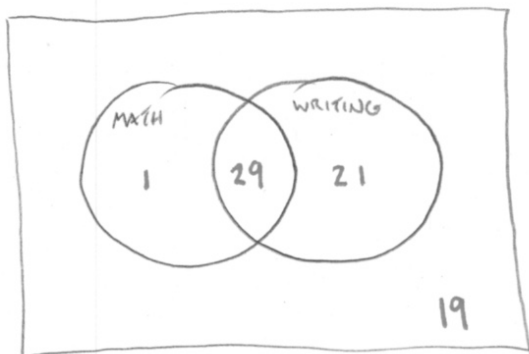
- 2 pts (b) How many people took more than one vacation? $3 + 4 + 6 + 4 = 17$

- 2 pts (c) How many people did not take a vacation during the Winter? $13 + 6 + 22 + 7 = 48$

- 5 pts 8. Draw a carefully labelled Venn diagram to represent the following data and answer to the following scenario.

In a survey of 70 first-year students, 30 were enrolled in a math course and 50 were enrolled in a writing course. Of those enrolled in the writing course, 21 weren't enrolled in a math course.

How many students in the survey were enrolled in neither a math course nor a writing course?



$$50 - 1 - 29 - 21 = 19$$

- 5 pts 9. The Consumer Price Index for the year 1970 was 38.8 and for the year 2012 was 229.6. If someone needed a \$30,000 annual salary to maintain a certain standard of living in 1970, how much would be needed to maintain the same standard of living in 2012?

$$30,000 \frac{\$}{1970} \cdot \frac{229.6 \frac{\$}{2012}}{38.8 \frac{\$}{1970}} = \boxed{177,525.77} \frac{\$}{2012}$$

- 4 pts 10. In October 2013, the national debt reached 17,075 billion dollars. Rewrite that amount in scientific notation.

$$1.7075 \times 10^4 \text{ BILLION} = 1.7075 \times 10^4 \times 10^9 \\ = \boxed{1.7075 \times 10^{13}}$$

4 pts

11. A person earns 6 times as much now as in the person's previous job. By what percent have their earnings increased?

500% INCREASE

e.g. $\frac{6-1}{1} \times 100\%$

4 pts

12. Identify at least one potential source of bias in the following study and explain your answer clearly.

To determine what percentage of New Englanders are Republicans, a political science researcher polls students at the University of Vermont.

UNIVERSITY OF VERMONT STUDENTS ARE NOT REPRESENTATIVE
OF THE POPULATION OF NEW ENGLANDERS.
SELECTION BIAS.

5 pts

13. The pass rate in one math course went from 60% last year to 70% this year. What was the relative change in pass rates?

$$\frac{70-60}{60} \times 100\% \approx 16.67\%$$

5 pts

14. Peru's population is about 30.4 million ^{in 2019} and its yearly growth rate was approximately 1.25%. If the growth rate stays constant, what will Peru's population be in 2100?

$$y = 30.4 \cdot 1.0125^x$$

x = # YEARS FROM 2019

2100 → x = 81

$$y = 30.4 \cdot 1.0125^{81} \approx 83.1517 \text{ MILLION}$$

83,151,700

8.31517×10^7

5 pts 15. Rubidium-82 has a half-life of 75 seconds. How much of a 5000 gram sample remains after 10 minutes?

$$10 \text{ min} \cdot \frac{60 \text{ sec}}{1 \text{ min}} = 600 \text{ sec}$$

$$y = A \left(\frac{1}{2}\right)^{x/T_{1/2}} \rightarrow y = 5000 \left(\frac{1}{2}\right)^{600/75} = \boxed{19.53125 \text{ g}}$$

16. Suppose gas costs \$3.40 per gallon, and your car averages 30 miles per gallon.

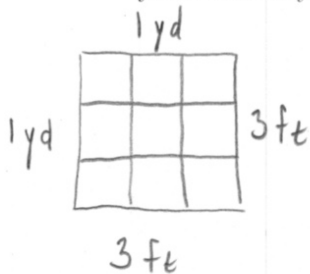
3 pts (a) How far can you go on \$150 worth of gas?

$$\cancel{\$150} \cdot \frac{\cancel{1 \text{ g}}}{\cancel{\$3.40}} \cdot \frac{30 \text{ mi}}{1 \cancel{\text{ g}}} = \boxed{1,323.5294 \text{ mi}}$$

3 pts (b) How much would it cost you to drive 3,000 miles to California?

$$3000 \text{ mi} \cdot \frac{1 \cancel{\text{ g}}}{30 \cancel{\text{ mi}}} \cdot \frac{\$3.40}{1 \cancel{\text{ g}}} = \boxed{\$340}$$

5 pts 17. How much would it cost to carpet an 6 foot by 11 foot room with carpeting that costs \$25 per square yard? Round your answer to the nearest dollar.



$$1 \text{ yd}^2 = 9 \text{ ft}^2$$

$$\text{Area} = 6 \text{ ft} \times 11 \text{ ft} = 66 \text{ ft}^2$$

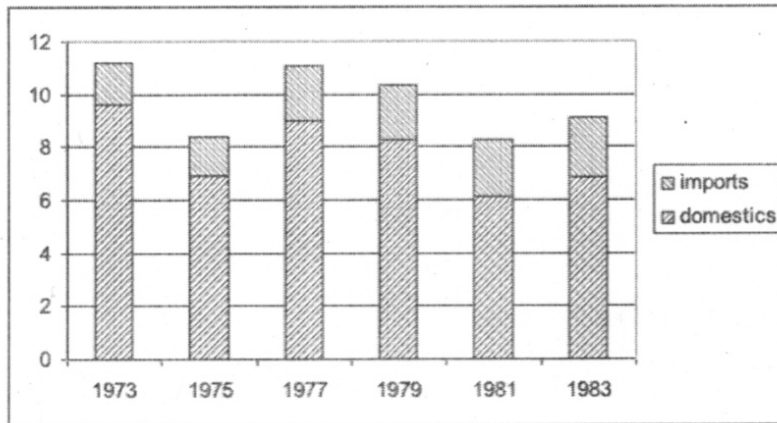
$$66 \text{ ft}^2 \cdot \frac{1 \cancel{\text{ yd}^2}}{9 \cancel{\text{ ft}^2}} \cdot \frac{\$25}{1 \cancel{\text{ yd}^2}} = \boxed{\$183.33}$$

5 pts

18. An amoeba cell is about 2.5×10^{-4} meters in length. If you were to line up 7 billion amoeba end-to-end, what is the total length? You must convert all numbers to scientific notation, calculate the length and leave the final answer in scientific notation, correct to two decimal places.

$$\begin{aligned}
 (2.5 \times 10^{-4}) \times (7 \times 10^9) &= (2.5 \times 7) \times (10^{-4} \times 10^9) \\
 &= 17.5 \times 10^5 = (1.75 \times 10) \times 10^5 \\
 &= \boxed{1.75 \times 10^6 \text{ m}}
 \end{aligned}$$

19. Consider the chart below depicting automobile sales (in millions) in the US for several years. Show the figures and calculations you're using to answer each question.



2 pts

(a) In 1977, domestic sales represented what percent of total sales?

$$\approx 80\%$$

2 pts

(b) Comparing 1973 and 1983, in which year did imports represent a greater percent of total sales?

1983

2 pts

(c) In which two-year period did total sales decrease the most? By what percent?

1973 - 1975
 $\approx 20-25\%$ DECREASE

~~$$\frac{8.2 - 10.6}{10.6} \times 100\% \approx -22.64\%$$~~