

### § 8.7 ESTIMATING THE DIFFERENCE BETWEEN TWO BINOMIAL PROPORTIONS

$$\left( \hat{P} = \frac{x}{n} \right)$$

ESSENTIALLY THE SAME

SAMPLING DISTRIBUTION OF  $(\hat{P}_1 - \hat{P}_2)$  HAS

$$\therefore \text{MEAN} = (\bar{P}_1 - \bar{P}_2)$$

$$\therefore \text{S.E.} = \sqrt{\frac{P_1 \bar{g}_1}{n_1} + \frac{P_2 \bar{g}_2}{n_2}} \approx \sqrt{\frac{\hat{P}_1 \hat{g}_1}{n_1} + \frac{\hat{P}_2 \hat{g}_2}{n_2}}$$

THE SAMPLING DISTRIBUTION FOR  $(\hat{P}_1 - \hat{P}_2)$  IS APPROXIMATELY

NORMALLY DISTRIBUTED IF

$$\begin{array}{ll} n_1 \hat{P}_1 > 5 & n_2 \hat{P}_2 > 5 \\ n_1 \hat{g}_1 > 5 & n_2 \hat{g}_2 > 5 \end{array}$$

$$\text{POINT ESTIMATION: } (\bar{P}_1 - \bar{P}_2) \approx (\hat{P}_1 - \hat{P}_2)$$

95% MARGIN OF ERROR:  $\pm 1.96 \text{ S.E.}$

$(1 - \alpha)$  CONFIDENCE INTERVAL:

$$(\hat{P}_1 - \hat{P}_2) \pm z_{\alpha/2} \text{ S.E.}$$

EX. # 55, 65