Directions Answer all questions in the space provided and box your final answers. Good luck! 1. (4 points) Which of the following is correct?

$$\cos(\cos^{-1}(\pi/2)) = \pi/2$$
 $\sin^{-1}(\sin(3\pi/2)) = 3\pi/2$ $\cos^{-1}(\cos(\pi/2)) = \pi/2$

2. (4 points) Find $(f^{-1})'(a)$, where $f(x) = 4x^5 + 2x - 1$ and a = 5.

3. (4 points) Suppose a sample of radioactive material takes 6 days to decay to 85% of its original mass. Assuming exponential decay, find the *half-life* of this material.

4. Differentiate the following functions. (e^x)

(a) (4 points)
$$f(x) = \ln\left(\frac{e^x}{x}\right)$$

(b) (4 points) $g(x) = \pi^{x^2}$

5. Evaluate the following integral.

$$\int_0^{\pi/2} \frac{\cos x}{4 + \sin^2 x} \, dx$$

6. Evaluate each of the following limits. $4r^2 + 3r - e^x$

(a) (4 points)
$$\lim_{x \to \infty} \frac{4x^2 + 3x - e^x}{3x^2 + e^x}$$

(b) (4 points)
$$\lim_{t \to \infty} \left(1 + \frac{1}{t} \right)^t$$