

### § 4.3 CALCULATING PROBABILITIES USING SIMPLE EVENTS

# 1, 2, 4, 5, 7-10, 14, 15

4.1 (a) SIMPLE EVENTS: 1, 2, 3, 4, 5, 6

(b) A: {2}

B: {2, 4, 6}

C: {3, 4, 5, 6}

D: {2}

E: {2, 4, 6}

F:  $\emptyset$  (EMPTY SET) = {}

(c)  $\frac{1}{6}$  EACH

(d) A:  $\frac{1}{6}$

D:  $\frac{1}{6}$

B:  $\frac{3}{6} = \frac{1}{2}$

E:  $\frac{3}{6} = \frac{1}{2}$

C:  $\frac{4}{6} = \frac{2}{3}$

F: 0

4.2 (a) REMEMBER THAT THE PROBABILITIES OF ALL SIMPLE EVENTS MUST ADD UP TO 1.

$$\therefore P(E_1) + P(E_2) + P(E_3) + P(E_4) + P(E_5) = 1$$

$$.15 + .15 + .4 + 2P(E_4) + P(E_5) = 1$$

$$.7 + 3P(E_5) = 1$$

$$3P(E_5) = .3$$

$$P(E_5) = .1 \quad \text{AND} \quad P(E_4) = 2P(E_5) = 2(.1) = .2$$

$$\therefore \boxed{\begin{array}{l} P(E_1) = .15 \quad P(E_2) = .15 \quad P(E_3) = .4 \\ P(E_4) = .2 \quad P(E_5) = .1 \end{array}}$$

$$(b) A = \{E_1, E_3, E_4\}$$

$$P(A) = P(E_1) + P(E_3) + P(E_4)$$

$$= .15 + .4 + .2 = .75$$

$$B = \{E_2, E_3\}$$

$$P(B) = P(E_2) + P(E_3)$$

$$= .15 + .4 = .55$$

$$(c) \{E_1, E_2, E_3, E_4\}$$

$$(d) \{E_3\}$$

4.4

$$(a) .49 + ? + .21 + .09 = 1$$

$$\Rightarrow ? = 1 - .49 - .21 - .09 = .21$$

$$(b) P(\text{HIT AT LEAST ONE})$$

$$= P(\text{HH, HM, or MH})$$

SIMPLE EVENTS

$$= P(\text{HH}) + P(\text{HM}) + P(\text{MH}) = .49 + .21 + .21 = .91$$

4.5 (a)  $S = \text{NDQ}, \text{DQH}, \text{NQH}, \text{NDH}$  ALL EQUALLY LIKELY

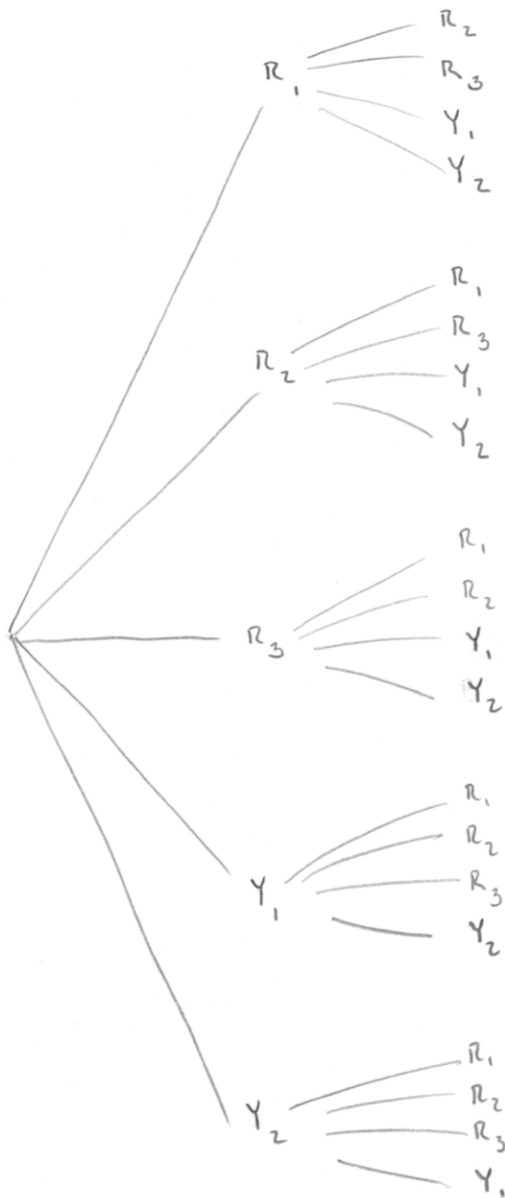
$$(b) P(\text{CONTAINS HALF DOLLAR}) = P(\text{DQH, NQH, or NDH})$$

$$= P(\text{DQH}) + P(\text{NQH}) + P(\text{NDH}) = \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = \frac{3}{4}$$

$$(c) P(\text{60¢ or more}) = P(DQH, NQH, NDH)$$

$$= P(DQH) + P(NQH) + P(NDH) = \boxed{\frac{3}{4}}$$

4.7



$$\therefore S = R_1 R_2, R_1 R_3, R_1 Y_1, R_1 Y_2, \\ R_2 R_1, R_2 R_3, R_2 Y_1, R_2 Y_2, \\ R_3 R_1, R_3 R_2, R_3 Y_1, R_3 Y_2, \\ Y_1 R_1, Y_1 R_2, Y_1 R_3, Y_1 Y_2, \\ Y_2 R_1, Y_2 R_2, Y_2 R_3, Y_2 Y_1$$

4.8 ADD  $R_1 R_1, R_2 R_2, R_3 R_3, Y_1 Y_1, Y_2 Y_2$

—————  
SAME BALL SELECTED TWICE.

4.9

(a)  $P(\text{NEED EYEGASSES})$

$$= P(\text{NEED GLASSES \& USE GLASSES}) + P(\text{NEED GLASSES \& DON'T USE GLASSES})$$

$$= .44 + .14 = \boxed{.58}$$

(b)  $P(\text{NEED GLASSES \& DON'T USE THEM}) = \boxed{.14}$

(c)  $P(\text{USE GLASSES}) = P(\text{NEED GLASSES, USE GLASSES}) + P(\text{DON'T NEED GLASSES, USE GLASSES})$

$$= .44 + .02 = \boxed{.46}$$

4.10

(a)  $S = 1, 2, 3, \dots, 35, 36, 0, 00$ .

(b) EACH SIMPLE EVENT EQUALLY LIKELY. 38 SIMPLE EVENTS.

$$\text{PROBABILITY OF EACH} = \frac{1}{38}$$

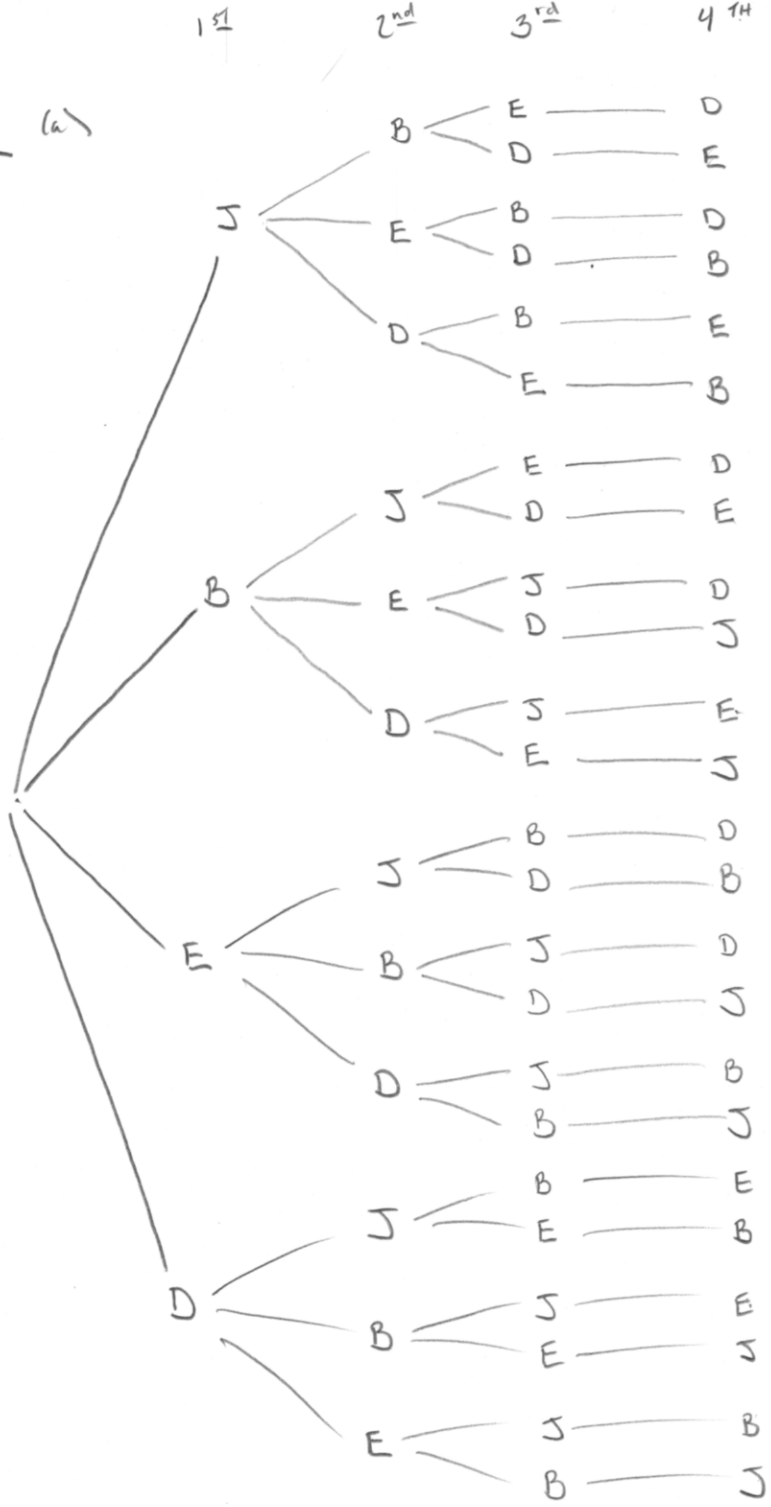
(c)  $A = \{0, 00\}$

$$P(A) = P(0) + P(00) = \frac{1}{38} + \frac{1}{38} = \frac{2}{38} = \boxed{\frac{1}{19}}$$

(d)  $P(1-18) = P(1) + P(2) + \dots + P(18)$

$$= 18 \times \frac{1}{38} = \frac{18}{38} = \boxed{\frac{9}{19}}$$

4.14 (a)



24 SIMPLE EVENTS  
IN SAMPLE SPACE

(b)  $\frac{1}{24}$

(c)  $\frac{6}{24} = \frac{1}{4}$

(d)  $\frac{2}{24} = \frac{1}{12}$

(e)  $\frac{6}{24} = \frac{1}{4}$

4.15

$$(a) P(\text{Normal Color, Normal Size}) = \frac{140}{300} = \boxed{\frac{7}{15}}$$

$$(b) P(\text{Vermillion Color})$$

$$= P(\text{Vermillion Color, Normal Size}) + P(\text{Vermillion Color, Mini Size})$$

$$= \frac{3}{300} + \frac{151}{300} = \frac{154}{300} = \boxed{\frac{77}{150}}$$

$$(c) P(\text{V. color, Mini Size, or Both})$$

$$= P(\text{V. color, Mini-Size}) + P(\text{V. color, Normal Size})$$

$$+ P(\text{Normal color, Mini-Size})$$

$$= \frac{151}{300} + \frac{3}{300} + \frac{6}{300} = \frac{160}{300} = \boxed{\frac{8}{15}}$$