

7.4 THE CENTRAL LIMIT THEOREM

DISTRIBUTION VS. SAMPLING DISTRIBUTION

OF INDIVIDUAL
MEASUREMENTS
TAKEN FROM POPULATION

OF AVERAGES (OR SUMS)
OF n MEASUREMENTS
TAKEN FROM POPULATION

1 EXPERIMENT IS INDIVIDUAL
MEASUREMENT

1 EXPERIMENT IS TAKING n MEASUREMENTS
AND AVERAGING (OR ADDING) THEM

COULD HAVE ANY SHAPE

IS APPROXIMATELY NORMAL

(UNDER CERTAIN ASSUMPTIONS
 • DISTRIBUTION IS NORMAL, OR
 • $n \geq 30$)

e.g. ROLLING A DIE

DISTRIBUTION IS
UNIFORM

SAMPLING DISTRIBUTION FOR
APPROXIMATELY NORMAL, EVEN FOR
 $n = 2, 3, 4, \dots$ (SMALL #'S)

CENTRAL LIMIT THM

IF RANDOM SAMPLES OF n OBSERVATIONS ARE DRAWN FROM A
NONNORMAL POPULATION WITH MEAN μ & STAND. DEV. σ , THEN FOR LARGE n
THE SAMPLING DISTRIBUTION OF THE SAMPLE MEAN \bar{x} IS APPROX. NORMALLY
DISTRIBUTED WITH MEAN μ (SAME!) AND STAND. DEV.

$$\frac{\sigma}{\sqrt{n}}$$

"STANDARD ERROR
OF THE MEAN" / S.E.M.
S.E.

(APPROX. GETS BETTER AS n GETS LARGER.)

C.L.T. CAN BE RESTATED TO APPLY TO THE SUM OF THE SAMPLE MEASUREMENTS
 $\sum x_i$, WHICH, AS n BECOMES LARGE ALSO HAS AN APPROX. NORMAL
DISTRIBUTION WITH MEAN $n\mu$ & STAND. DEV. $5\sqrt{n}$

§7.5 THE SAMPLING DISTRIBUTION OF THE SAMPLE MEAN

EXAMPLES.

TACK AHEAD #17

*25, 28, 30, 31