

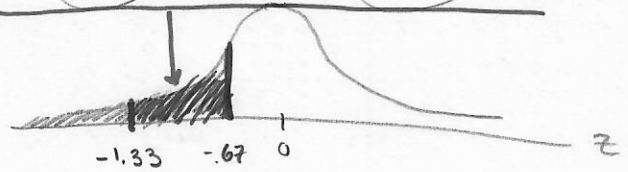
$$P(1.00 < X < 1.10)$$

$$z = \frac{x - \mu}{\sigma}$$

$$P\left(\frac{1.00 - 1.2}{.15} < z < \frac{1.10 - 1.2}{.15}\right)$$

$$P(-1.33 < z < -.67)$$

ROUNDING



LEFT OF  $-.67$ , NOT LEFT OF  $-1.33$

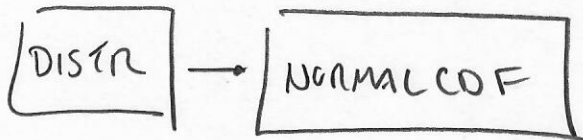
$$P(z < -.67) - P(z < -1.33)$$

$$.2514 - .0918$$

$$= \underline{\underline{.1596}} \approx .1613$$

close!

CALCULATOR:



$$\text{NORMALCDF} \left( \overset{\text{LEFT}}{\text{LOWER BOUND}}, \overset{\text{RIGHT}}{\text{UPPER BOUND}}, \mu, \sigma \right)$$

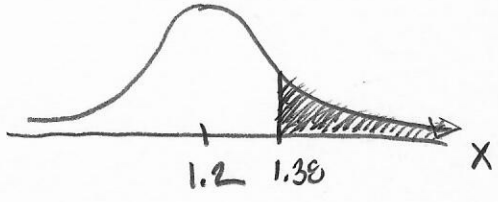
1

$$P(x > 1.38)$$

$$z = \frac{x - \mu}{\sigma}$$

Normalcdf (left, right,  $\mu$ ,  $\sigma$ )

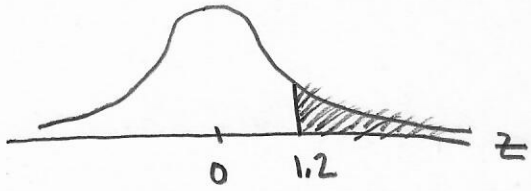
$$P(z > \frac{1.38 - 1.2}{.15})$$



$$= P(z > 1.2) = 1 - P(z < 1.2)$$

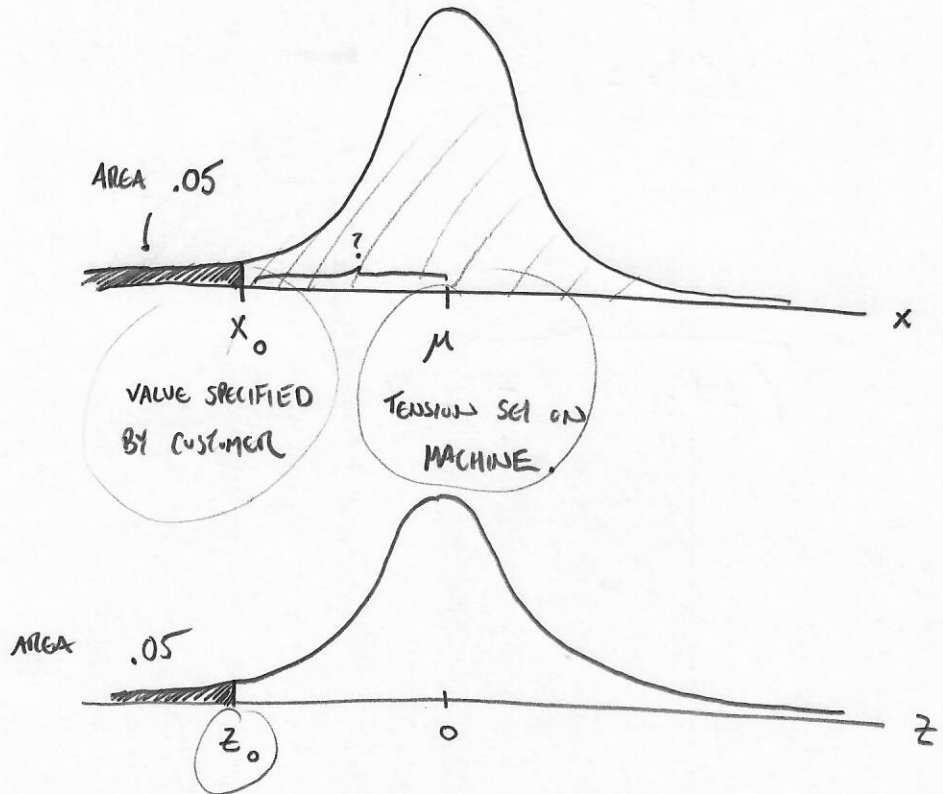
1) switch (pew.

2) 1 - prob.



$$= 1 - .8849 = .1151$$

X NORMAL RANDOM VARIABLE  
= STRING TENSION ACHIEVED.



LOOK UP PROB. 0.05 IN BODY OF TABLE 2  
TO FIND  $z_0 = -1.645$

i.e.  $z_0$  IS 1.645 STAND. DEV. BELOW MEAN

$\Rightarrow X_0$  IS 1.645 STAND DEV. BELOW MEAN

$$X_0 = \mu - 1.645 \sigma$$

$$X_0 = \mu - 1.645(2) + 1.645(2)$$

$$\underline{X_0} + 1.645(2) = \mu$$

$$X_0 + 3.29 = \mu$$

3.29 PSI ABOVE VALUE.

## §6.4 THE NORMAL APPROXIMATION TO THE BINOMIAL PROBABILITY DISTRIBUTION.

Let  $X$  be a BINOMIAL RANDOM VARIABLE.

$n$  TRIALS (INDEPENDENT, IDENTICAL)

PROB. OF SUCCESS  $p$ , PROB. OF FAILURE  $q = 1 - p$ .

$X = \#$  SUCCESSES IN  $n$  TRIALS.

RECALL:  $X$  HAS MEAN / EXPECTED VALUE  $\mu = np$

AND STANDARD DEV  $\sigma = \sqrt{npq}$

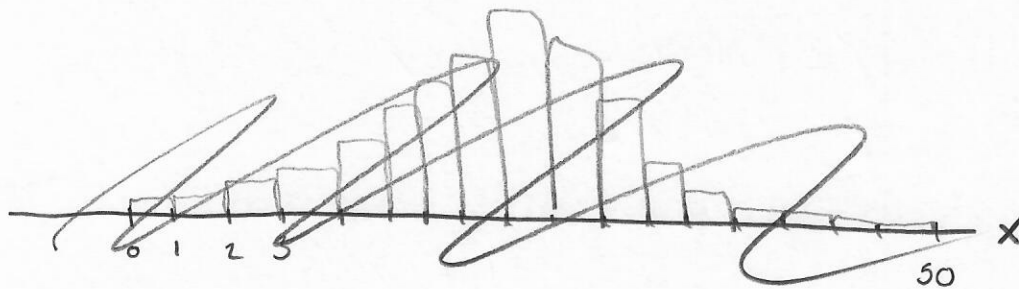
FOR ANY DISCRETE R.V.

$$\mu = \sum x p(x)$$

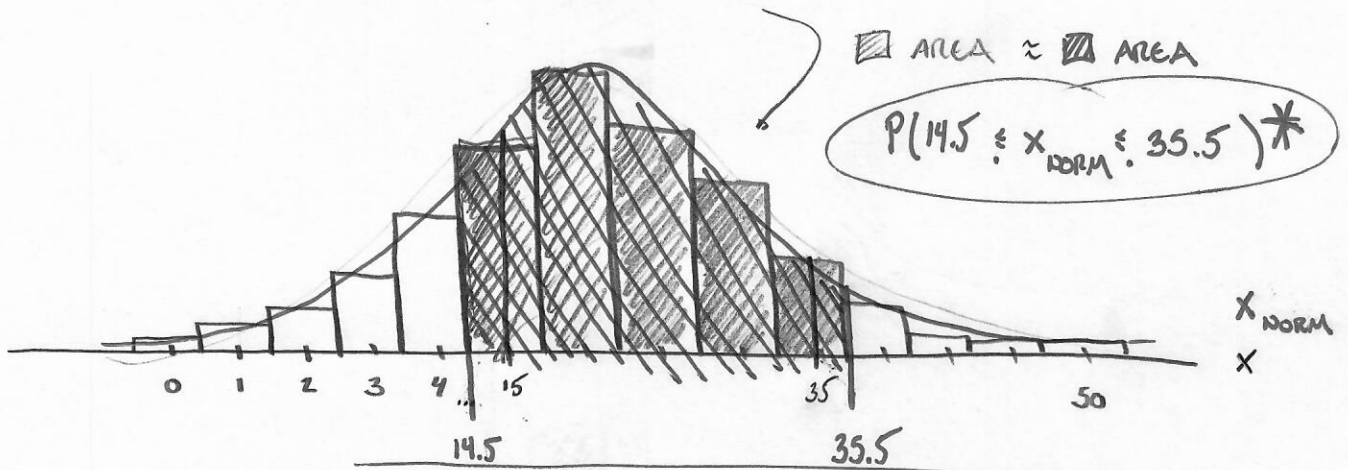
DON'T NEED  
TO MEMORIZE

$$\sigma = \sqrt{\sum (x - \mu)^2 p(x)}$$

ex. SUPPOSE  $X$  IS BINOMIAL R.V.  $X$  WITH  $n = 50$ ,  $p = .4$ .  
FIND  $P(15 \leq X \leq 35)$



$$P(15 \leq X \leq 35)$$



FACT: THE PROBABILITY DISTR. FOR  $X$  (BINOMIAL, DISCRETE)  
IS APPROXIMATELY NORMAL

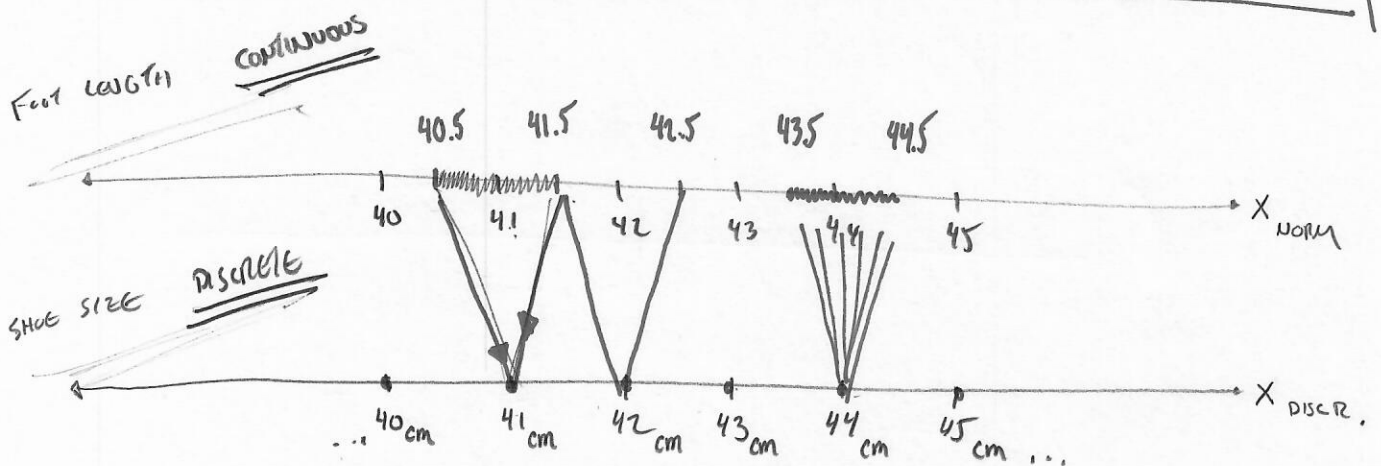
WITH

$$\mu = np$$

$$\sigma = \sqrt{npq}$$

AS LONG AS  $n$  IS LARGE & NEITHER  
 $p$  NOR  $q$  IS TOO SMALL.

\* RULE OF THUMB:  $np \geq 5$ ,  $nq \geq 5$  \*



$$* P(14.5 \leq X_{\text{NORM}} \leq 35.5)$$



↑

$$\mu = np = (50)(.4) = 20$$

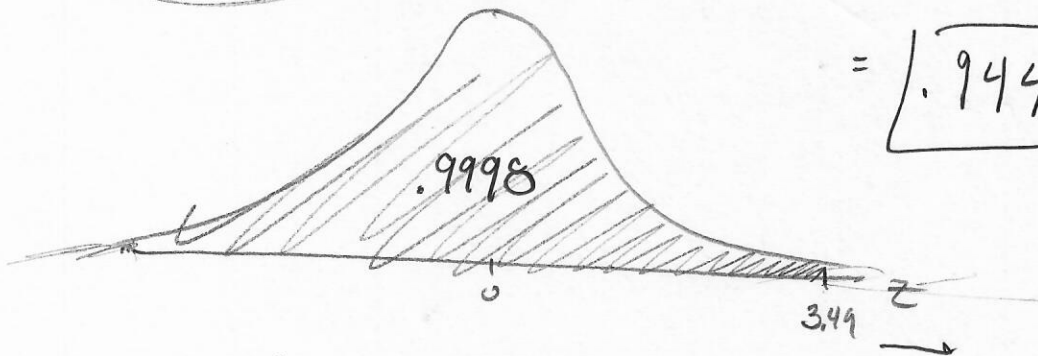
$$\sigma = \sqrt{npq} = \sqrt{(50)(.4)(.6)} = \sqrt{12} \approx 3.4641$$

$$P\left(\frac{14.5 - 20}{3.4641} \leq Z \leq \frac{35.5 - 20}{3.4641}\right)$$

$$= P(-1.59 \leq Z \leq 4.47)$$

$$= P(Z \leq 4.47) - P(Z \leq -1.59) = 1 - .0559$$

$$= \boxed{.9441}$$



$$P(Z \leq z_0) = \begin{cases} 0 & \text{if } z_0 \leq -3.49 \\ \text{TABLE} & \text{if } -3.49 \leq z_0 \leq 3.49 \\ 1 & \text{if } z_0 \geq 3.49 \end{cases} \quad P(Z \leq 4.47) \approx 1$$

EX.

EXPERIMENT: FLIP A COIN 500 TIMES.

(ASSUME SUCCESS = HEADS &  $P(\text{SUCCESS}) = p = .5$ )

$X = \#$  HEADS.

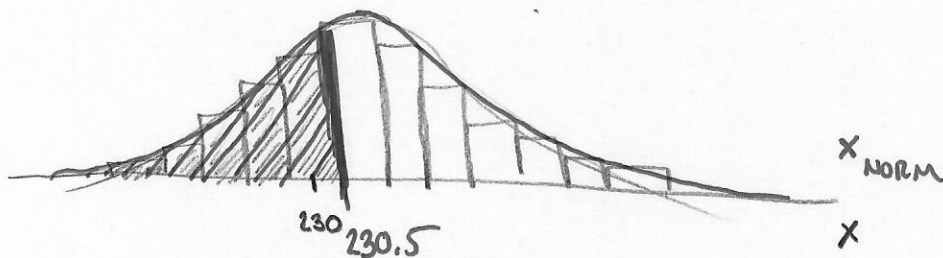
$$n = 500$$

$$p = .5$$

$$\text{FIND } P(X \leq 230) = P(X=0) + P(X=1) + \dots + P(X=230)$$

$$C_0^{500} (.5)^0 (.5)^{500} + \dots + C_{230}^{500} (.5)^{230} (.5)^{270}$$

BINOMIAL PROB. DISTR.



$X_{\text{NORM}}$  AND  $X$  ARE

$$\mu = np = (500)(.5) = 250$$

$$\sigma = \sqrt{npq} = \sqrt{(500)(.5)(.5)}$$

$$= \sqrt{125} = 11.1803$$

$$P(X \leq 230) = \boxed{\phantom{.0409}} = \boxed{\phantom{.0409}} = P(X_{\text{NORM}} \leq \underline{230.5})$$

§6.3

$$= P\left(z \leq \frac{230.5 - 250}{11.1803}\right)$$

$$z = \frac{x - \mu}{\sigma}$$

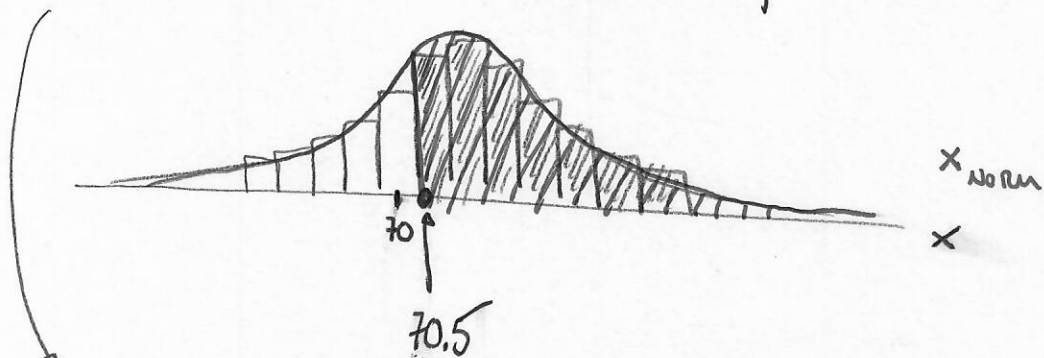
$$= P(z \leq -1.74) = \boxed{.0409}$$



ex. BASEBALL PLAYER WITH CAREER BATTING AVERAGE OF .281  
 GOES TO BATTING 300 TIMES IN A SEASON.  
 FIND THE PROBABILITY THAT SHE GETS A HIT MORE  
 THAN 70 TIMES.

BINOMIAL EXP:  $n = 300$   $q = 1 - p$   
 $p = .281$  ( $q = .719$ )  
 $X = \# \text{ successes (HITS)}$

FIND  $P(X > 70) = P(X \geq 71)$



$\approx P(X_{\text{NORM}} \geq 70.5)$

$\mu = np = (300)(.281) = 84.3$

$\sigma = \sqrt{npq} = \sqrt{(300)(.281)(.719)}$   
 $= 7.7854$

$z = \frac{x - \mu}{\sigma}$

$P\left(z \geq \frac{70.5 - 84.3}{7.7854}\right)$

$= P(z \geq -1.77) = 1 - P(z \leq -1.77)$

$= 1 - .0384 = \boxed{.9616}$