Name: $\qquad$
Each question is worth 5 points. Show your work in the space provided and write your final answer neatly on the answer line. Good luck!

1. Simplify $\left(3+\frac{1}{4}\right)\left(1-\frac{4}{5}\right)$.
2. 
3. Simplify $\left(\frac{1+\frac{1}{4}}{1+4}\right)^{2}$.
4. $\qquad$
5. Simplify $\left(\frac{x^{8} y^{-4}}{16 y^{4 / 3}}\right)^{-1 / 4}$ and eliminate any negative exponents.
6. $\qquad$
7. Evaluate $\left(\frac{4}{9}\right)^{-3 / 2}$.
8. 
9. Factor $-3 x^{3}+6 x^{2}-3 x$ completely.
10. $\qquad$
11. Perform the division $\frac{x+3}{4 x^{2}-9} \div \frac{x^{2}+7 x+12}{2 x^{2}+7 x-15}$ and simplify.
12. 
13. Perform the addition $\frac{1}{x+3}+\frac{1}{x^{2}-9}$ and simplify.
14. 
15. Find all real solutions of the equation $x^{2}=2 x+15$.
16. 
17. Factor $x^{4}-1$ completely.
18. 
19. Solve the equation $P=2 l+2 w$ for $w$.
20. 
21. Solve the inequality $x^{2}<3(x+6)$. Expres your answer using interval notation.
22. 
23. Find all real solutions of the equation $1+\sqrt{6-x}=x-3$.
24. $\qquad$
25. Find the radius of the circle with the equation $x^{2}+y^{2}+6 y+2=0$.
26. $\qquad$
27. Find the $y$-intercept of the line that passes through the points $(1,1)$ and $(5,-1)$.
28. $\qquad$
29. Evaluate and simplify $\frac{f(a+h)-f(a)}{h}$ when $f(x)=2 x^{2}+5 x-4$.
30. 
31. Find the domain of the function $g(x)=\frac{\sqrt{2+x}}{3-x}$. Express your answer using interval notation.
32. 
33. The graph $y=f(x)$ is shown below. List the intervals (if any) on which $f$ is increasing.

34. 
35. Use the graph from the previous question to approximate
(a) the net change in $f$ from -2 to 2 , and
(b) the average rate of change in $f$ from -2 to 2 .
36. $\qquad$
37. Sketch the graph $y=|x+1|+x$ by first completing the table of values below and then plotting points. State the domain and range of $f$ using interval notation on the answer line.

| $x$ | $y$ |
| :---: | :---: |
| -4 |  |
| -3 |  |
| -2 |  |
| -1 |  |
| 0 |  |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |


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19. $\qquad$
20. Sketch the graph of the piecewise defined function $f(x)=\left\{\begin{array}{ll}2 x+3 & \text { if } x<1 \\ 3-x & \text { if } x \geq 1\end{array}\right.$ below.

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