Name: $\qquad$
Each question is worth 5 points. Show your work in the space provided and put a box around your final answer. Answers should be simplified, but can include logarithmic and/or exponential expressions. Good luck!

1. Sketch the graph of $f(x)=2-\sqrt{x+1}$. Label any/all $x$-intercepts, $y$-intercepts, horizontal asymptotes, and vertical asymptotes. State the domain and range using interval notation.

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2. Suppose $f(x)=2 x^{2}+x$ and $g(x)=3-x$. Find $f(g(x))$ and $g(f(x))$.
3. Let $f$ be the one-to-one function $f(x)=\frac{3}{x-4}$. Find $f^{-1}(x)$.
4. Use the following table to evaluate $g\left(f^{-1}(2)\right)$.

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 1 | 4 | 3 | 0 | 2 | 5 |
| $g(x)$ | 4 | 2 | 3 | 1 | 5 | 0 |

5. Consider the quadratic function $q(x)=x^{2}-12 x+40$. Use "completing the square" to write $q(x)$ in standard form. Then determine the maximum/minimum value of $q(x)$ and state whether it is a maximum or a minimum.
6. Find the maximum/minimum value of $f(x)=-\frac{x^{2}}{3}+2 x+7$ and state whether it is a maximum or minimum.
7. Let $y=-7 x^{5}-x^{4}+5 x+2$. Describe the end behavior of $f$ by filling in the blanks:

As $x \rightarrow-\infty, y \rightarrow \longrightarrow$.

As $x \rightarrow \infty, y \rightarrow$ $\qquad$
8. Sketch the graph of the polynomial $P(x)=-\frac{2}{3} x^{2}(x-4)$. Label any/all $x$-intercepts, $y$-intercepts, horizontal asymptotes, and vertical asymptotes. Make sure your graph exhibits the proper end behavior and correctly shows where $P(x)$ is positive/negative.

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9. Solve: $7^{1-2 x}=7^{3 x-5}$.
10. Solve $8 e^{x / 3}=40$.
11. Solve: $\frac{50}{1+e^{-x}}=4$.
12. Sketch the graph of $f(x)=2+4^{-x}$. Label any/all $x$-intercepts, $y$-intercepts, horizontal asymptotes, and vertical asymptotes. State the domain and range using interval notation.

13. Evaluate $\log _{2}\left(\frac{1}{32}\right)$.
14. Use $\log$ laws to evaluate $3 \ln (2)+2 \ln (3)-\ln (72)$.
15. Sketch the graphs of all three of the following functions on the same set of axes below. Label any/all $x$-intercepts, $y$-intercepts, horizontal asymptotes, and vertical asymptotes.

$$
\begin{aligned}
f(x) & =x \\
g(x) & =e^{x} \\
h(x) & =\ln (x)
\end{aligned}
$$

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16. Let $f(x)=\ln (1-6 x)$. State the domain of $f$ using interval notation.
17. Sketch the graph of $f(x)=-\log _{5}(x-3)$. Label any/all $x$-intercepts, $y$-intercepts, horizontal asymptotes, and vertical asymptotes. State the domain and range using interval notation.

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18. Solve: $2 \ln (x)=\ln (2)+\ln (3 x-4)$.
19. Solve: $\log _{5}(x+1)-\log _{5}(x-1)=2$.
20. Solve: $\log (x+2)+\log (x-1)=1$.
